

ANSWER KEY TO THE MOCK FINAL EXAM

NOTE: this answer key contains only the correct answers. To get full credit for your solutions, you also need to show the procedure you used to arrive at the correct answer, unless explicitly stated in the exercise.

Exercise 1 (8 points).

- (a) 2.
- (b) 1.
- (c) 2.
- (d) $+\infty$.

Exercise 2 (4 points). 1 Solution.

$$\begin{aligned} \lim_{x \rightarrow -\infty} f(x) &= -\infty, & \lim_{x \rightarrow \infty} f(x) &= +\infty. \\ f(-1) &= 5, & f(1) &= 1. \end{aligned}$$

Exercise 3 (16 points).

$$\begin{aligned} \lim_{x \rightarrow -\infty} f(x) &= -\infty, & \lim_{x \rightarrow +\infty} f(x) &= +\infty. \\ \lim_{x \rightarrow 5^-} f(x) &= -\infty, & \lim_{x \rightarrow 5^+} f(x) &= +\infty. \\ f(3) &= 1, & f(7) &= 9. \\ \text{Ran}(f) &= \{ y \mid y \leq 1 \text{ OR } y \geq 9 \}. \end{aligned}$$

Exercise 4 (16 points). Decreasing between -3 and -2 , and between 0 and 2 . Increasing between -2 and 0 and between 2 and 3 . Absolute maxima at -3 and 3 , local maxima at 0 . Absolute minima at -2 and 2 , local minima at -2 and 2 . CU between -3 and $-\frac{2}{3}\sqrt{3}$, and between $\frac{2}{3}\sqrt{3}$ and 3 . CD between $-\frac{2}{3}\sqrt{3}$ and $\frac{2}{3}\sqrt{3}$. Inflection points at $-\frac{2}{3}\sqrt{3}$ and $\frac{2}{3}\sqrt{3}$.

Exercise 5 (16 points).

(a) $\frac{15}{4}$.

(b) $\frac{1}{4}\pi$.

(c) $\frac{1}{2}\ln 2$.

(d) $-\frac{31}{25} + \frac{32}{5}\ln 2$.

(e) $\frac{1}{6}$.

Exercise 6 (8 points). $\frac{9}{2}$.